

- T5S.3: (a)  $N_A = 100$   $N_B = 100$   $U = 200\varepsilon$
- 2.8271E+192/3.0330E+144=0.9321134E+48
  - 70–130 include 0.99983854 of states
  - 3.6469E+146/3.0330E+144=1.202407E+2
- (b)  $N_A = 1000$   $N_B = 1000$   $U = 2000\varepsilon$  (request 2001 rows)
- 6.748E+1949/1.844E+1459=3.659436E490
  - 904–1096 include 0.99981572 of states
  - 2.213E+1462/1.844E+1459=1.200109E3

much increased relative probability of being in central state; likely spread  $\delta U_A$  increased on an absolute basis, but not on relative basis.

- (c)  $N_A = 1000$   $N_B = 1000$   $U = 200\varepsilon$  (request 201 rows)
- 7.9768E+380/2.2201E+323=3.592991E57
  - 73–127 include 0.99988206 of states
  - 4.1639E+325/2.2201E+323=1.875546E2

modest changes toward more central probability

- (d)  $N_A = 100$   $N_B = 100$   $U = 2000\varepsilon$  (request 2001 rows)
- 3.5051E+605/1.9303E+384=1.815832E221
  - 828–1172 include 0.999805788 of states
  - 5.0377E+386/1.9303E+384=2.609802E2

much increased relative probability of being in central state; likely spread  $\delta U_A$  increased on an absolute basis, but not on relative basis.

Note the online error list <http://www.physics.pomona.edu/sixideas/errfiles/sierrt3.html> suggests doing all these problems with MaxRow 200, but I've followed the instructions as given in the hard copy. Below are the results for the default MaxRows (201)

- (b)  $N_A = 1000$   $N_B = 1000$   $U = 2009\varepsilon$  (request 201 rows)
- 1.722E+1956/1.020E+1485=1.688235E471
  - 0.4552–0.5448 include 0.9997597 of states
  - 1.964E+1504/1.020E+1485=1.92549E19
- (d)  $N_A = 100$   $N_B = 100$   $U = 2009\varepsilon$  (request 201 rows)
- 3.6635E+607/1.2200E+401=3.002869E206
  - 0.4154–0.5846 include 0.9998342 of states
  - 8.5681E+413/1.2200E+401=7.023033E12

- T5S.8: (a)  $\Delta S = 0.00000001 \text{ J/K} = k_B \ln(\Omega_1/\Omega_2)$

$$\begin{aligned} \ln(\Omega_1/\Omega_2) &= 0.00000001/k_B = 7.2429 \times 10^{14} \\ \log_{10}(\Omega_1/\Omega_2) &= 7.2429 \times 10^{14}/\ln(10) = 3.1456 \times 10^{14} \\ \Omega_1/\Omega_2 &= 10^{3.1456 \times 10^{14}} \end{aligned}$$

- (b) I'm willing to bet that I'll never see something with those odds happen.

T5R.1: Call space alien object  $A$  (so  $\Omega_A$  increases if  $U_A$  decreases) and normal object  $B$  (so  $\Omega_B$  increases if  $U_B$  increases). Both  $\Omega_A$  and  $\Omega_B$  will increase (so then  $\Omega_{AB} = \Omega_A \Omega_B$  will also increase) if energy flows from  $A$  to  $B$ . So as long as the hypothesis hold, less energy in  $A$  (and hence more in  $B$ ) will increase total entropy—hence  $A$  will reach 'equilibrium' (i.e., steady state) only after it has expelled all of its energy into  $B$ . It doesn't matter if  $B$  is a flame or an ice bath—both are 'normal' cases where  $\Omega_B$  will increase if  $U_B$  increases.  $A$  might be said to have an infinite temperature (since heat will flow from it into any normal body) but in fact the usual definition of temperature will find a negative value (so  $\Delta S = Q/T$  is positive for  $Q < 0$ ).